



软件分析

动态符号执行和抽象解释

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提醒

- 下周上课前为课程项目组队截止日期



复习：符号执行

- 请列举符号执行不能得到精确结果的场景
- 有循环的情况
- 分支太多，在有限时间内探索不完的情况
- 约束求解失败的情况



约束求解失败的情况

- 形成了复杂条件
 - $x^5 + 3x^3 == y$
 - p->next->value == x
- 调用了系统调用
 - If (file.read()==x)
- 动态符号执行
 - 混合程序的真实执行和符号执行
 - 在约束求解无法进行的时候，用真实值代替符号值
 - 如果真实值x=10，则 $x^5 + 3x^3 == y$ 变为103000==y，可满足



动态符号执行

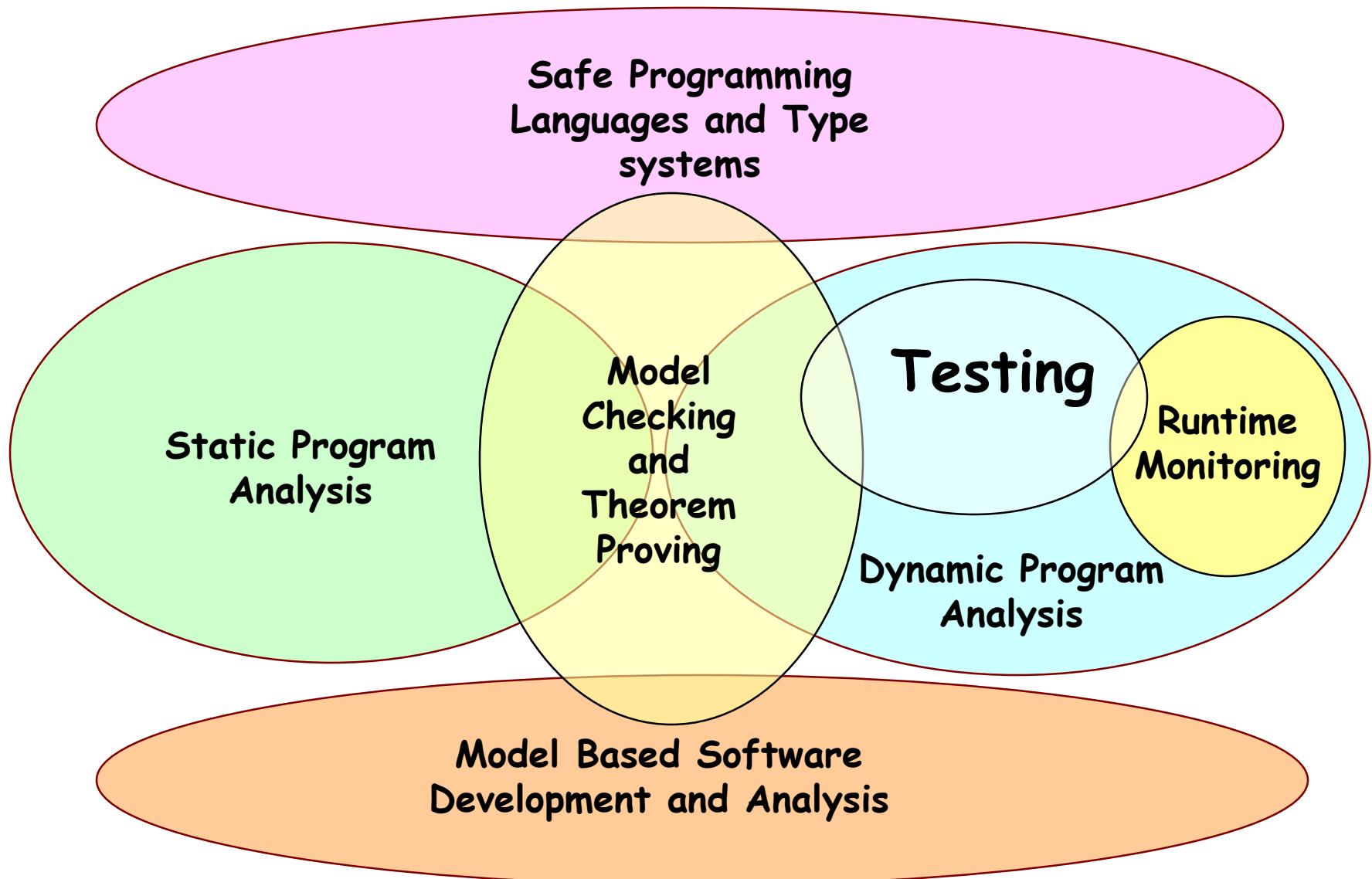
- 动态符号执行主要用于生成测试输入
- 代表性工作：
 - Concolic Testing, Koushik Sen
 - 主要工具：CUTE
 - Execution-Generated Testing, Cristian Cadar
 - 主要工具：KLEE

DART and CUTE: Concolic Testing

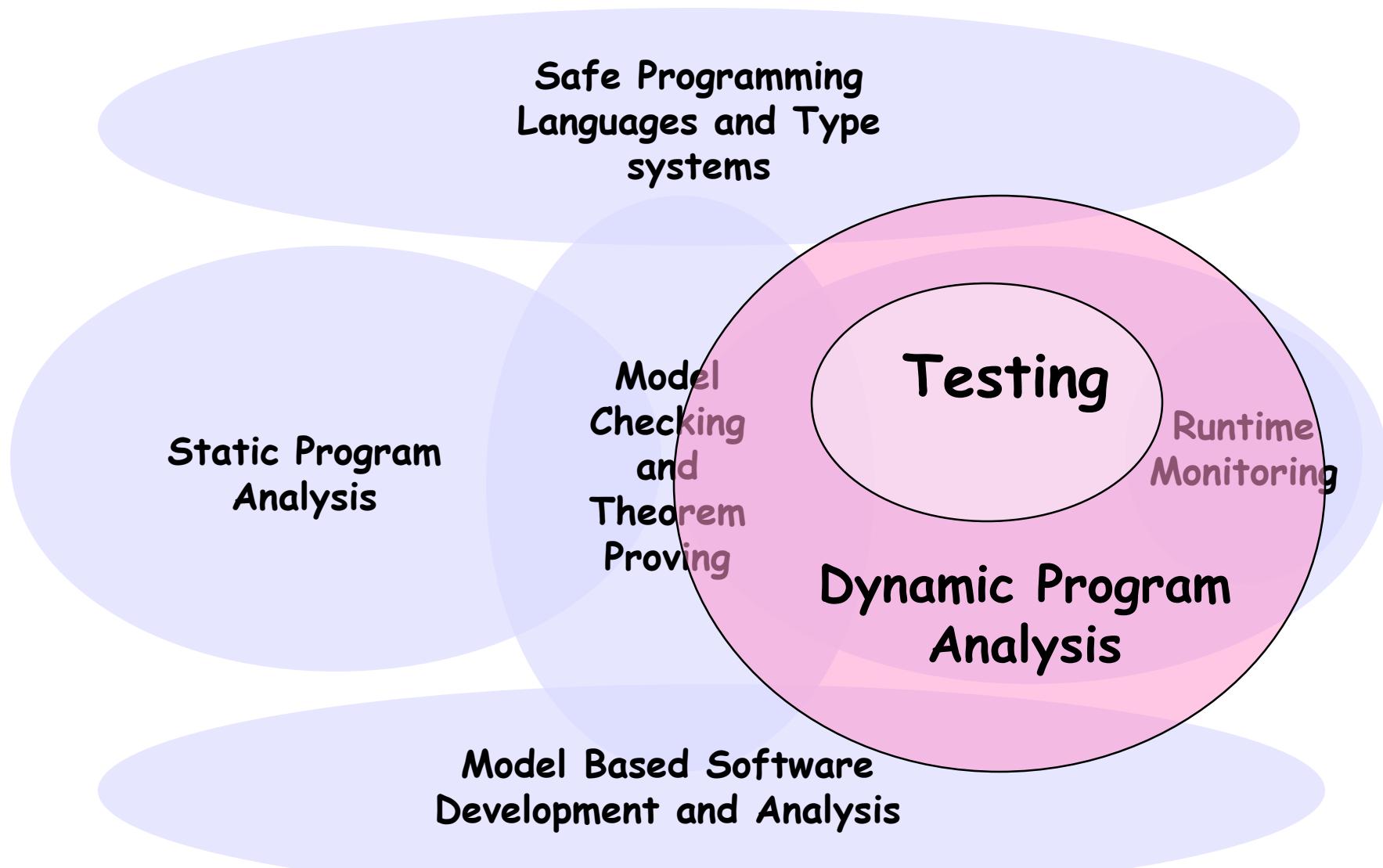
Koushik Sen
University of California, Berkeley

Joint work with Gul Agha, Patrice Godefroid, Nils Klarlund,
Rupak Majumdar, Darko Marinov

Big Picture



Big Picture



A Familiar Program: QuickSort

```
void quicksort (int[] a, int lo, int hi) {  
    int i=lo, j=hi, h;  
    int x=a[(lo+hi)/2];  
  
    // partition  
    do {  
        while (a[i]<x) i++;  
        while (a[j]>x) j--; if (i<=j) {  
            h=a[i];  
            a[i]=a[j];  
            a[j]=h;  
            i++;  
            j--;  
        }  
    } while (i<=j);  
  
    // recursion  
    if (lo<j) quicksort(a, lo, j);  
    if (i<hi) quicksort(a, i, hi);  
}
```

A Familiar Program: QuickSort

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            h=a[i];  
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            i++;  
            j--;  
        }  
    } while (i<=j);  
  
    // recursion  
    if (lo<j) quicksort(a, lo, j);  
    if (i<hi) quicksort(a, i, hi);  
}
```

- Test QuickSort
 - Create an array
 - Initialize the elements of the array
 - Execute the program on this array
- How much confidence do I have in this testing method?
- Is my test suite *Complete*?
- Can someone generate a small and *Complete* test suite for me?

Automated Test Generation

- Studied since 70's
 - King 76, Myers 79
- 30 years have passed, and yet no effective solution
- **What Happened???**

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 - Program-analysis techniques were expensive
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 - Program-analysis techniques were expensive
 - Automated theorem proving and constraint solving techniques were not efficient
- In the recent years we have seen remarkable progress in static program-analysis and constraint solving
 - SLAM, BLAST, ESP, Bandera, Saturn, MAGIC

Automated Test Generation

- Studied since 70's

King 70 Myers 70

Question: Can we use similar techniques in Automated Testing?

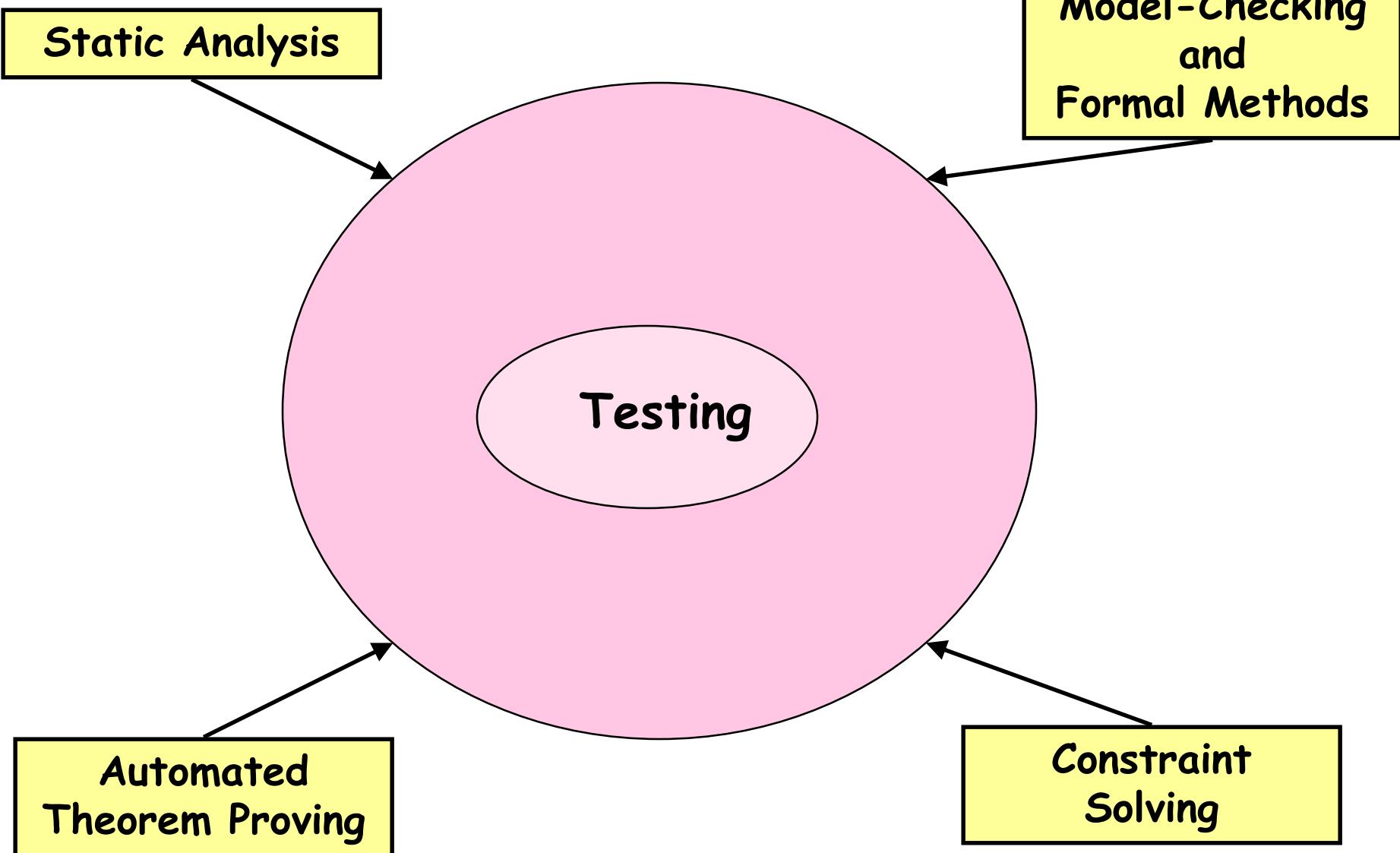
- What Happened???

- Program-analysis techniques were expensive
 - Automated theorem proving and constraint solving techniques were not efficient

- In the recent years we have seen remarkable progress in static program-analysis and constraint solving

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Systematic Automated Testing



CUTE and DART

- Combine **random testing** (concrete execution) and **symbolic testing** (symbolic execution)

[PLDI'05, FSE'05, FASE'06, CAV'06, ISSTA'07,
ICSE'07]

Concrete + Symbolic = Concolic

Goal

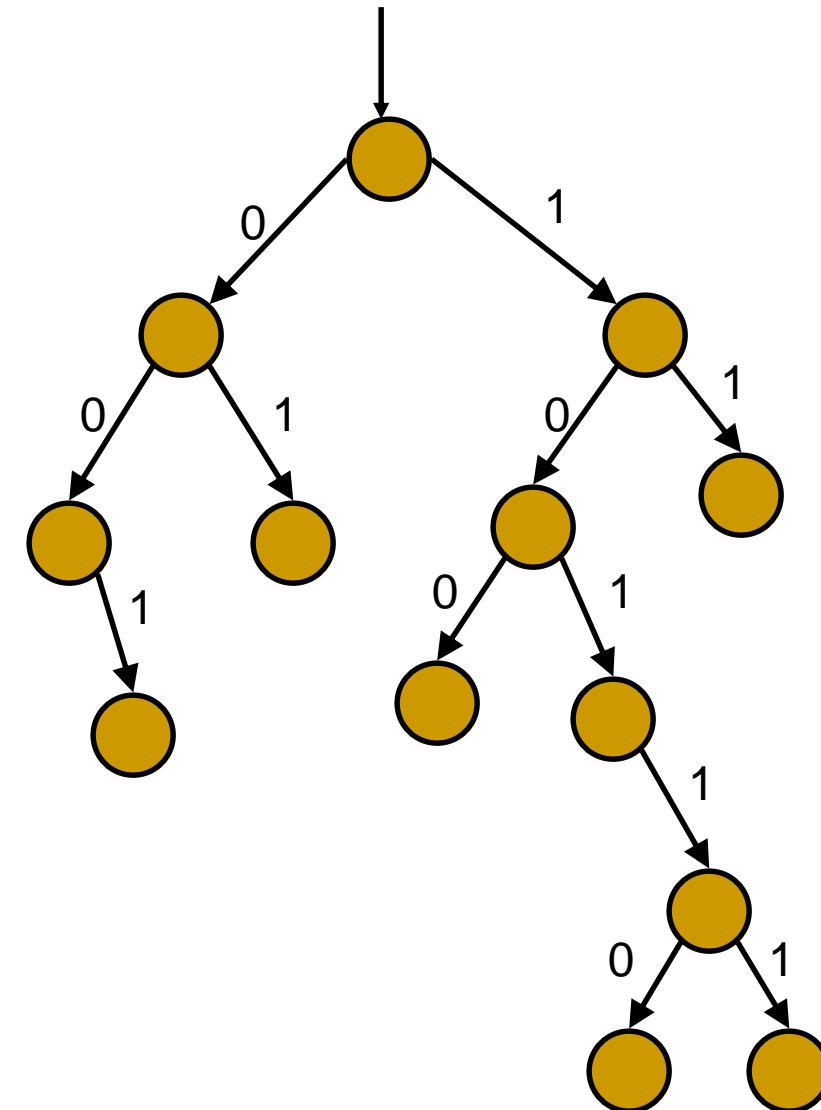
- Automated Unit Testing of real-world C and Java Programs
 - Generate test inputs
 - Execute unit under test on generated test inputs
 - so that all reachable statements are executed
 - Any assertion violation gets caught

Goal

- Automated Unit Testing of real-world C and Java Programs
 - Generate test inputs
 - Execute unit under test on generated test inputs
 - so that all reachable statements are executed
 - Any assertion violation gets caught
- Our Approach:
 - Explore all execution paths of an Unit for all possible inputs
 - Exploring all execution paths ensure that all reachable statements are executed

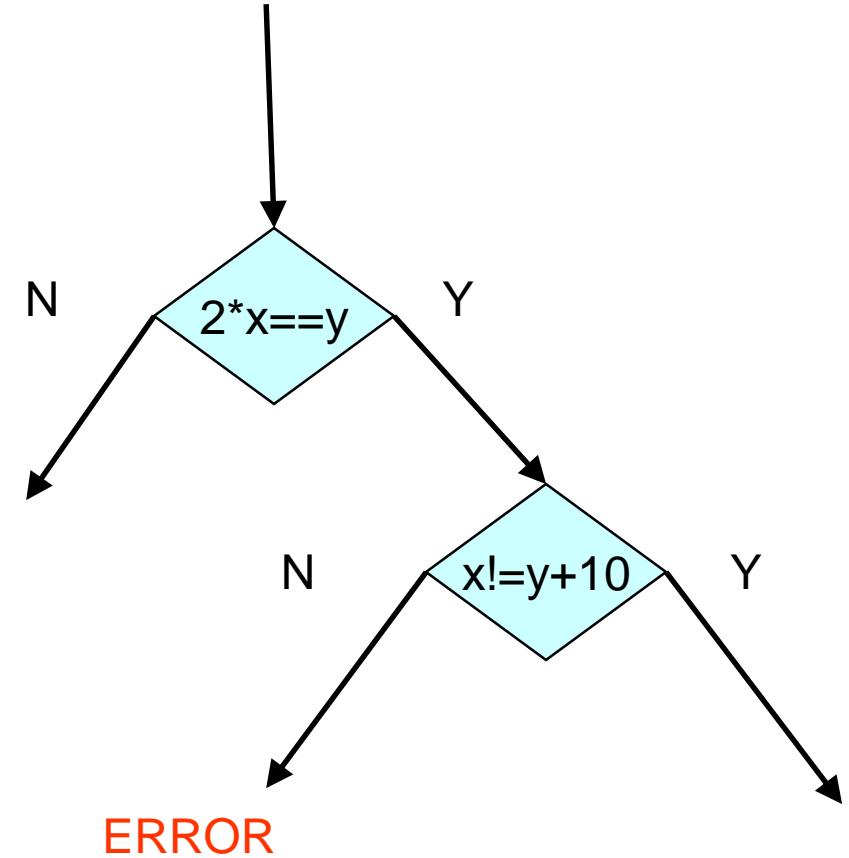
Execution Paths of a Program

- Can be seen as a **binary tree** with possibly infinite depth
 - Computation tree
- Each **node** represents the execution of a “**if then else**” statement
- Each **edge** represents the execution of a sequence of non-conditional statements
- Each path in the tree represents an equivalence class of inputs



Example of Computation Tree

```
void test_me(int x, int y) {  
    if(2*x==y){  
        if(x != y+10){  
            printf("I am fine here");  
        } else {  
            printf("I should not reach here");  
            ERROR;  
        }  
    }  
}
```



Concolic Testing: Finding Security and Safety Bugs

Divide by 0 Error

$x = 3 / i;$

Buffer Overflow

$a[i] = 4;$

Concolic Testing: Finding Security and Safety Bugs

**Key: Add Checks Automatically and
Perform Concolic Testing**

Divide by 0 Error

```
if (i !=0)
    x = 3 / i;
else
    ERROR;
```

Buffer Overflow

```
if (0<=i && i < a.length)
    a[i] = 4;
else
    ERROR;
```

Existing Approach I

- Random testing
 - generate random inputs
 - execute the program on generated inputs
- Probability of reaching an error can be astronomically less

```
test_me(int x){  
    if(x==94389){  
        ERROR;  
    }  
}
```

Probability of hitting
ERROR = $1/2^{32}$

Existing Approach II

- **Symbolic Execution**
 - use symbolic values for input variables
 - execute the program symbolically on symbolic input values
 - collect symbolic path constraints
 - use theorem prover to check if a branch can be taken
- **Does not scale** for large programs

```
test_me(int x){  
    if((x%10)*4!=17){  
        ERROR;  
    } else {  
        ERROR;  
    }  
}
```

Symbolic execution will say both branches are reachable:

False positive

Existing Approach II

- **Symbolic Execution**
 - use symbolic values for input variables
 - execute the program symbolically on symbolic input values
 - collect symbolic path constraints
 - use theorem prover to check if a branch can be taken
- **Does not scale** for large programs

```
test_me(int x){  
    if(bbox(x)!=17){  
        ERROR;  
    } else {  
        ERROR;  
    }  
}
```

Symbolic execution will say both branches are reachable:

False positive

Concolic Testing Approach

```
int double (int v) {  
  
    return 2*v;  
}  
  
void testme (int x, int y) {  
  
    z = double (y);  
  
    if (z == x) {  
  
        if (x > y+10) {  
  
            ERROR;  
        }  
    }  
}
```

- Random Test Driver:
 - random value for x and y
- Probability of reaching **ERROR** is extremely low

Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

$x = 22, y = 7$

Symbolic
Execution

symbolic
state

$x = x_0, y = y_0$

path
condition



Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```



```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

x = 22, y = 7,
z = 14

Symbolic
Execution

symbolic
state

x = x_0 , y = y_0 ,
z = 2^*y_0

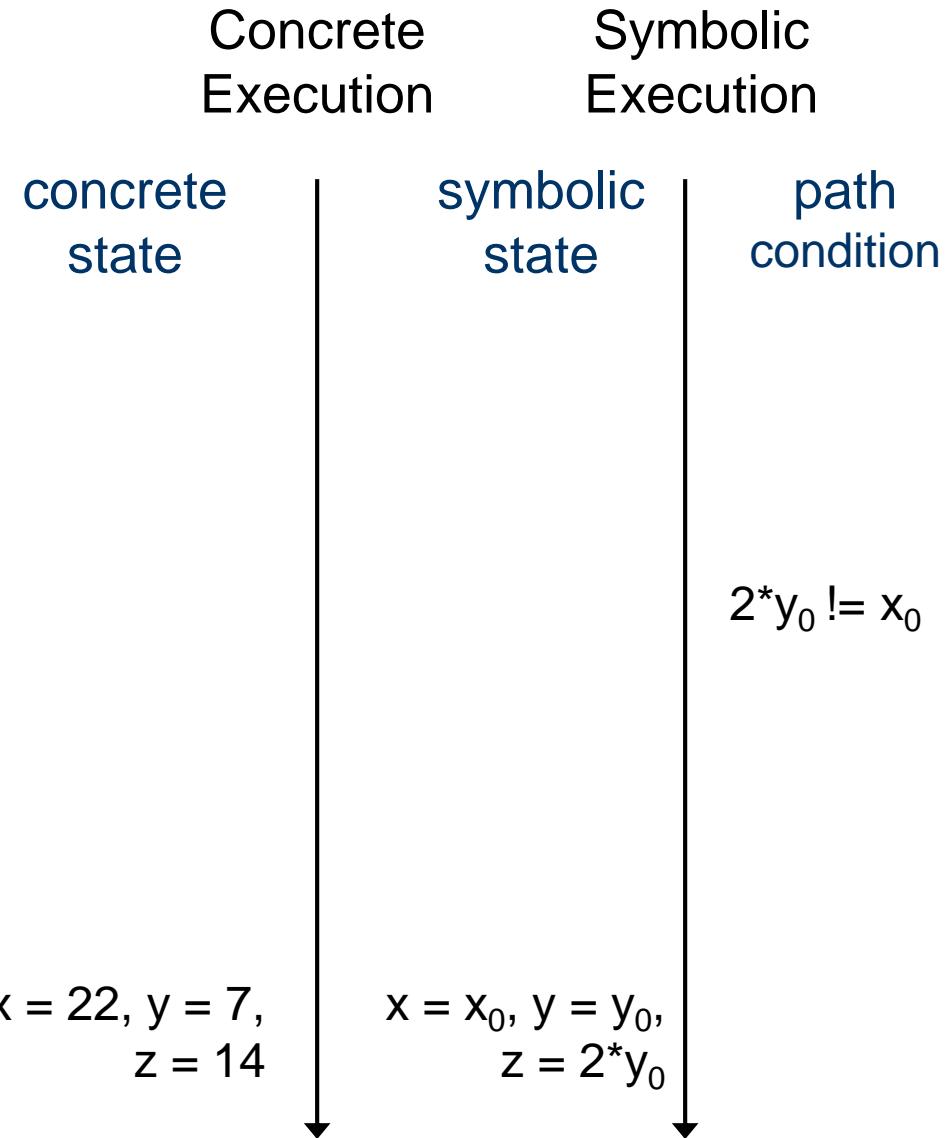
path
condition



Concolic Testing Approach

```
int double (int v) {  
    return 2*v;  
}
```

```
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    z = double (y);  
  
    if (z == x) {  
  
        if (x > y+10) {  
  
            ERROR;  
        }  
    }  
}
```



Concolic Testing Approach

```
int double (int v) {  
    return 2*v;  
}
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```
void testme (int x, int y) {  
    z = double (y);  
  
    if (z == x) {
```

```
        if (x > y+10) {
```

ERROR;

```
}
```

```
}
```

Concrete
Execution

Symbolic
Execution

path
condition

concrete
state

symbolic
state

Solve: $2^*y_0 == x_0$

Solution: $x_0 = 2, y_0 = 1$

$x = 22, y = 7,$
 $z = 14$

$x = x_0, y = y_0,$
 $z = 2^*y_0$

Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

$x = 2, y = 1$

Symbolic
Execution

symbolic
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$x = x_0, y = y_0$

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Concolic Testing Approach

```
int double (int v) {
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    return 2*v;
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void testme (int x, int y) {
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    z = double (y);
```



```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
    }
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

$x = 2, y = 1,$
 $z = 2$

Symbolic
Execution

symbolic
state

$x = x_0, y = y_0,$
 $z = 2^*y_0$

path
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Concolic Testing Approach

```
int double (int v) {
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```
    return 2*v;
```

```
}
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```
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```
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```
    if (z == x) {
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```
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```

```
            ERROR;
```

```
}
```

```
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```

Concrete
Execution

concrete
state

$x = 2, y = 1,$
 $z = 2$

Symbolic
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path
condition

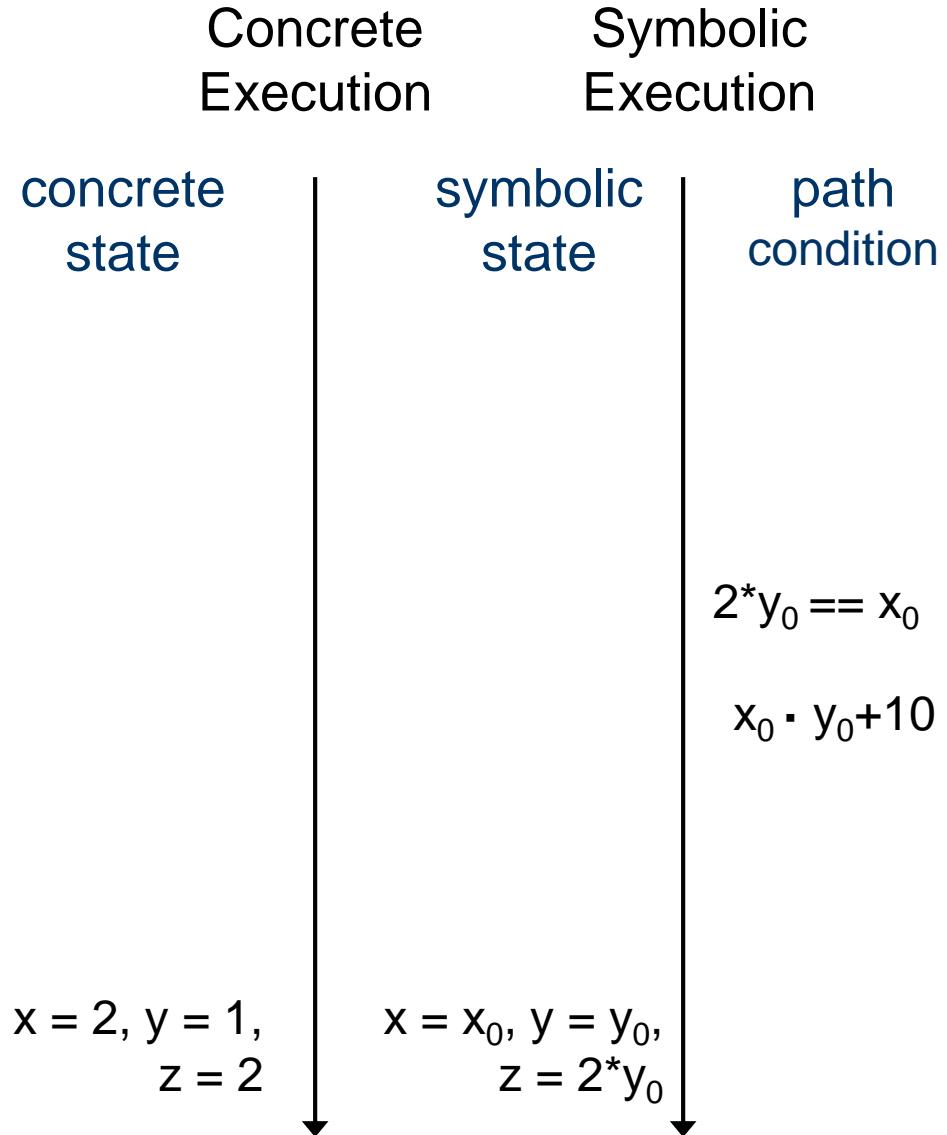
$2^*y_0 == x_0$



Concolic Testing Approach

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}
```

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    z = double (y);  
  
    if (z == x) {  
        if (x > y+10) {  
  
            ERROR;  
        }  
    }  
}
```



Concolic Testing Approach

```
int double (int v) {  
    return 2*v;  
}
```

```
void testme (int x, int y) {  
    z = double (y);
```

```
    if (z == x) {  
        if (x > y+10) {  
            ERROR;  
        }  
    }  
}
```

Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

path
condition

Solve: $(2^*y_0 == x_0) \wedge (x_0 > y_0 + 10)$

Solution: $x_0 = 30, y_0 = 15$

$2^*y_0 == x_0$

$x_0 > y_0 + 10$

$x = 2, y = 1,$
 $z = 2$

$x = x_0, y = y_0,$
 $z = 2^*y_0$

}



Concolic Testing Approach

```
int double (int v) {
```

```
    return 2*v;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = double (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

$x = 30, y = 15$

Symbolic
Execution

symbolic
state

$x = x_0, y = y_0$

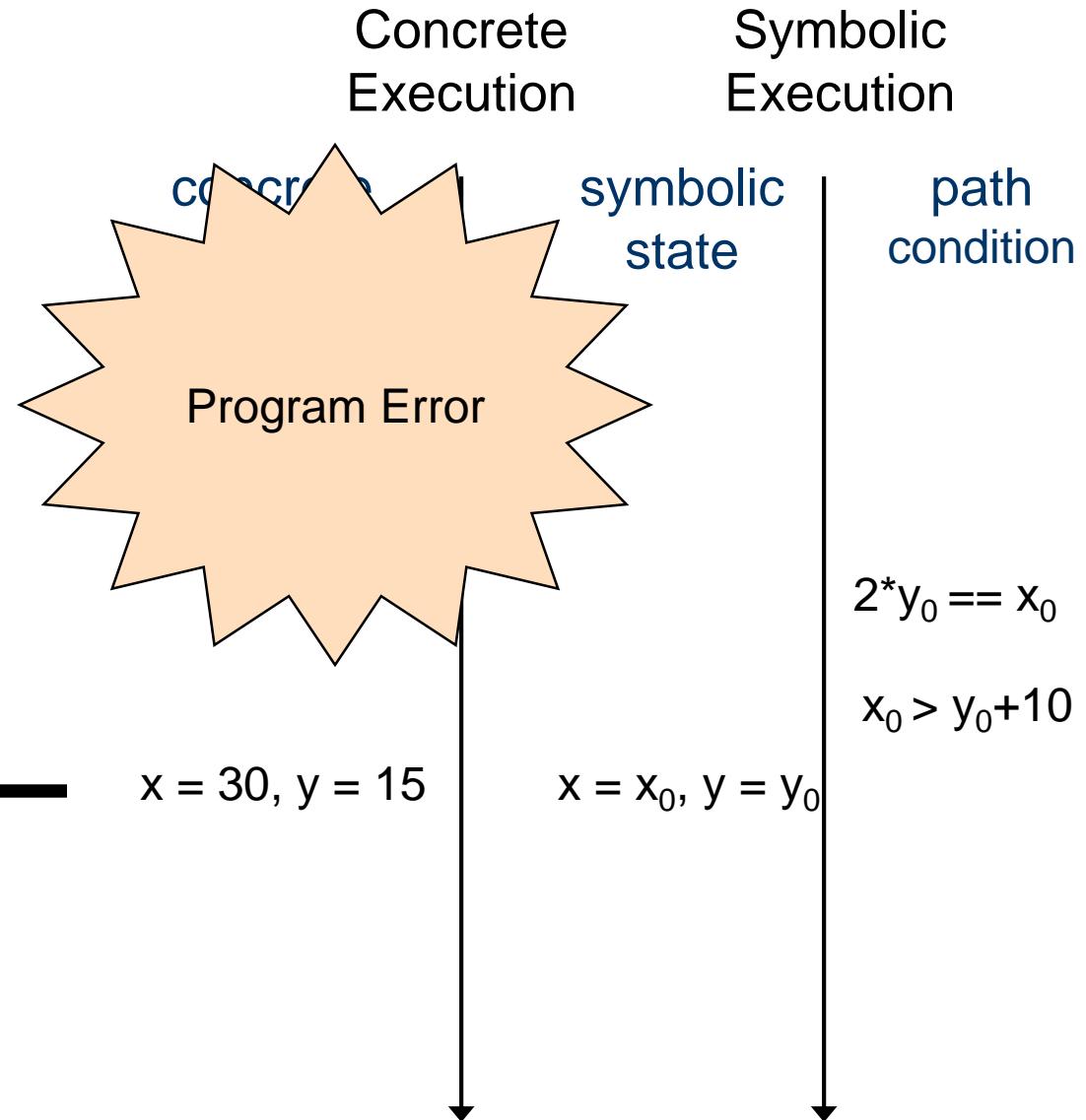
path
condition



Concolic Testing Approach

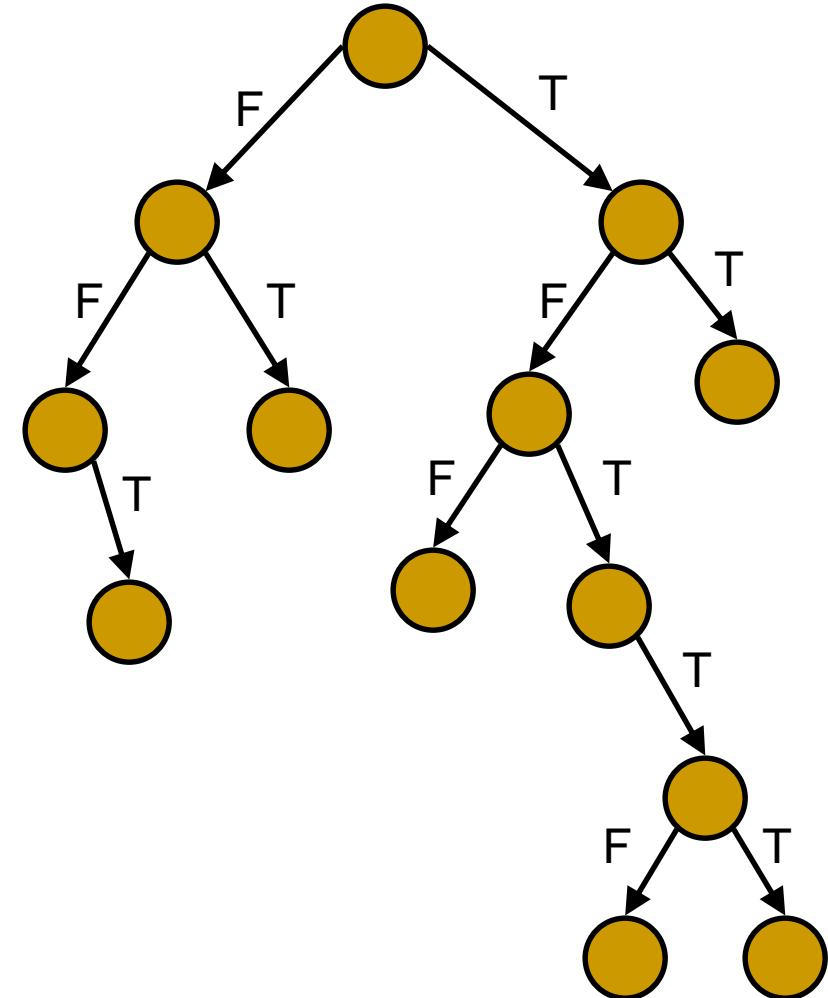
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void testme (int x, int y) {  
    z = double (y);  
  
    if (z == x) {  
  
        if (x > y+10) {  
  
            ← ERROR;  
        }  
    }  
}
```



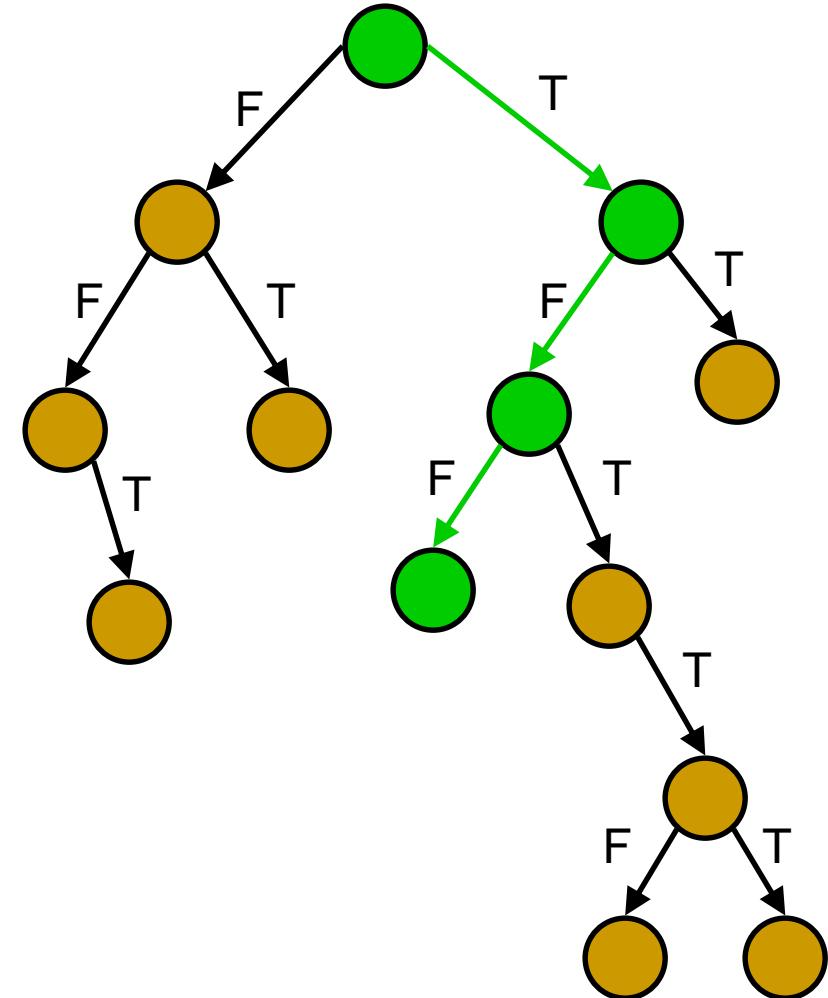
Explicit Path (not State) Model Checking

- Traverse all execution paths one by one to detect errors
 - assertion violations
 - program crash
 - uncaught exceptions
- combine with valgrind to discover memory errors



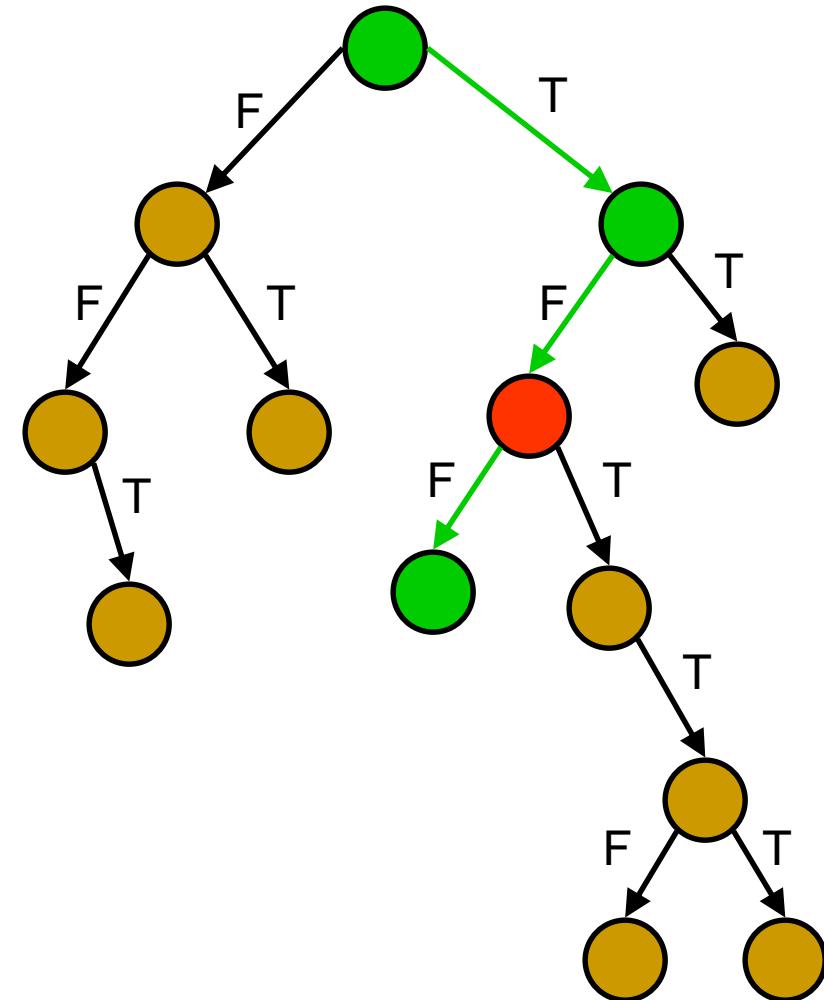
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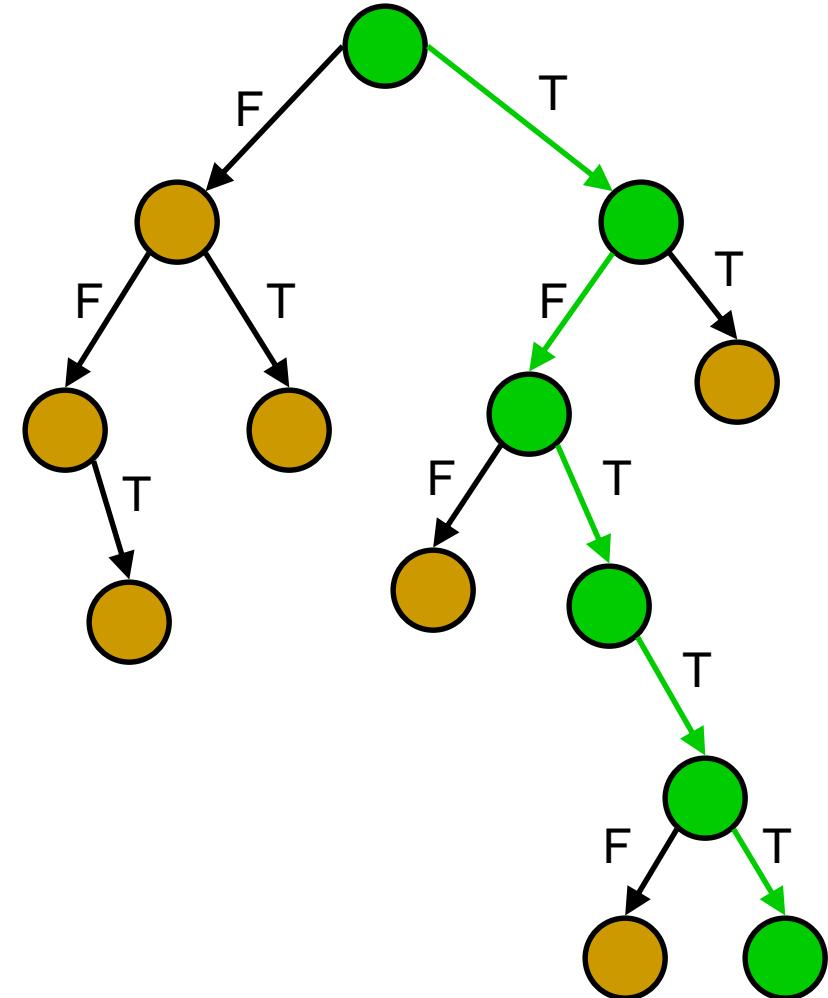
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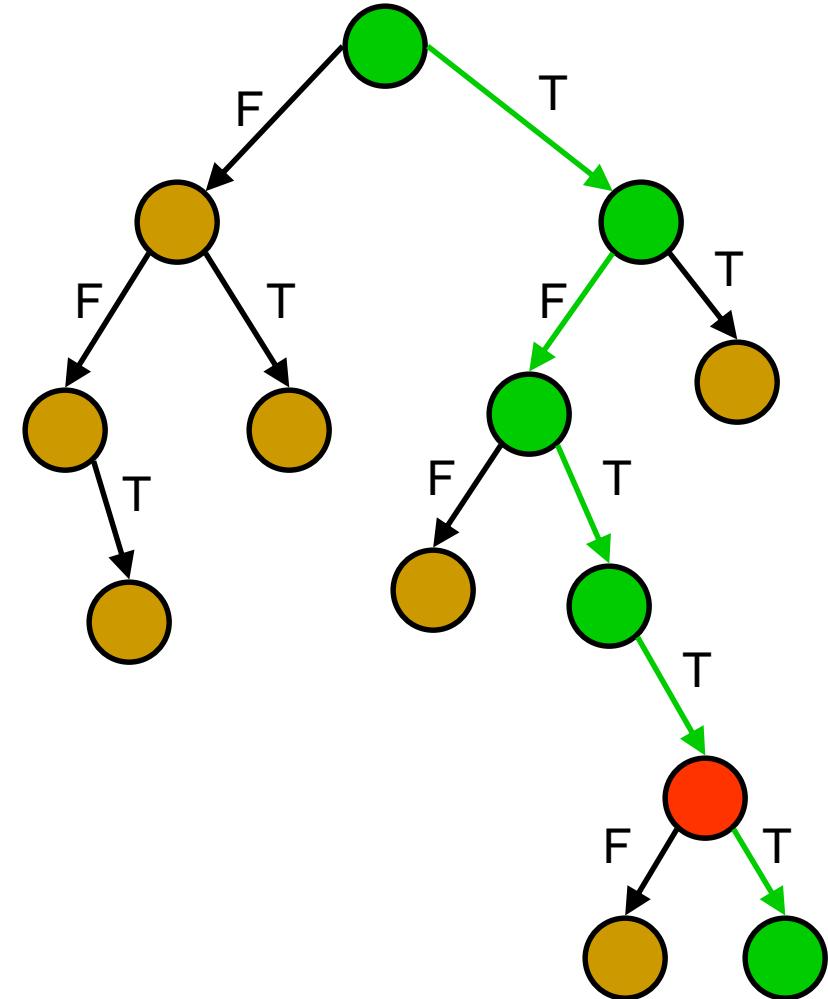
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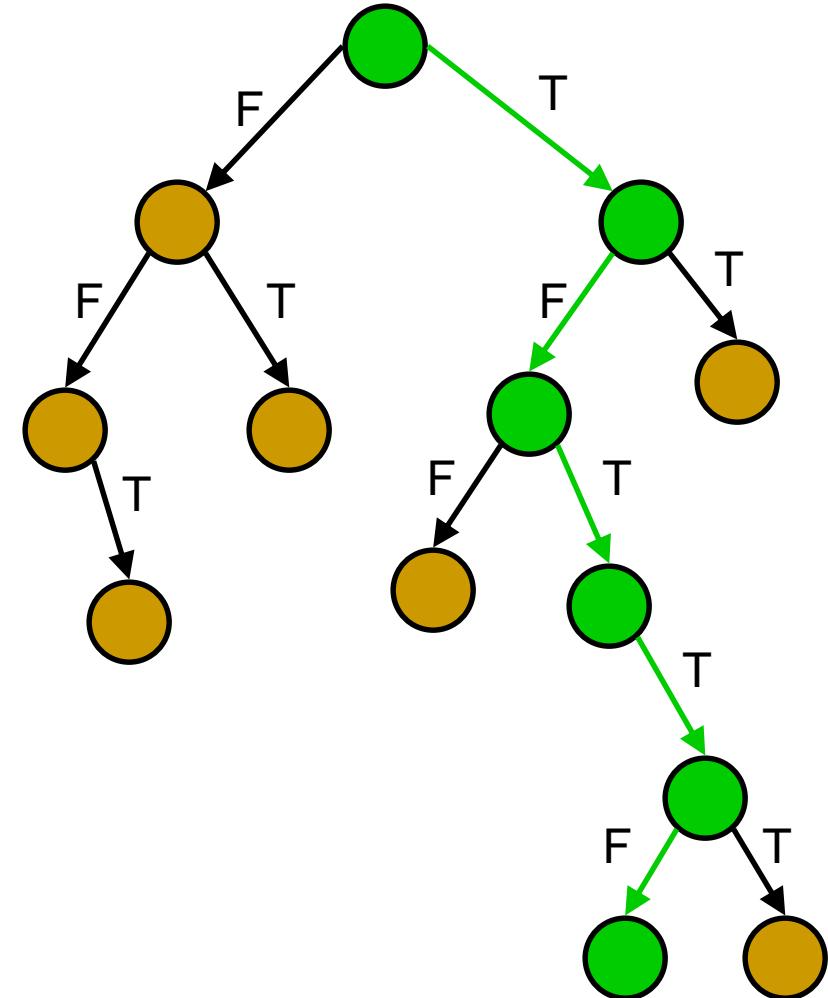
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- combine with valgrind to discover memory errors



Novelty : Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

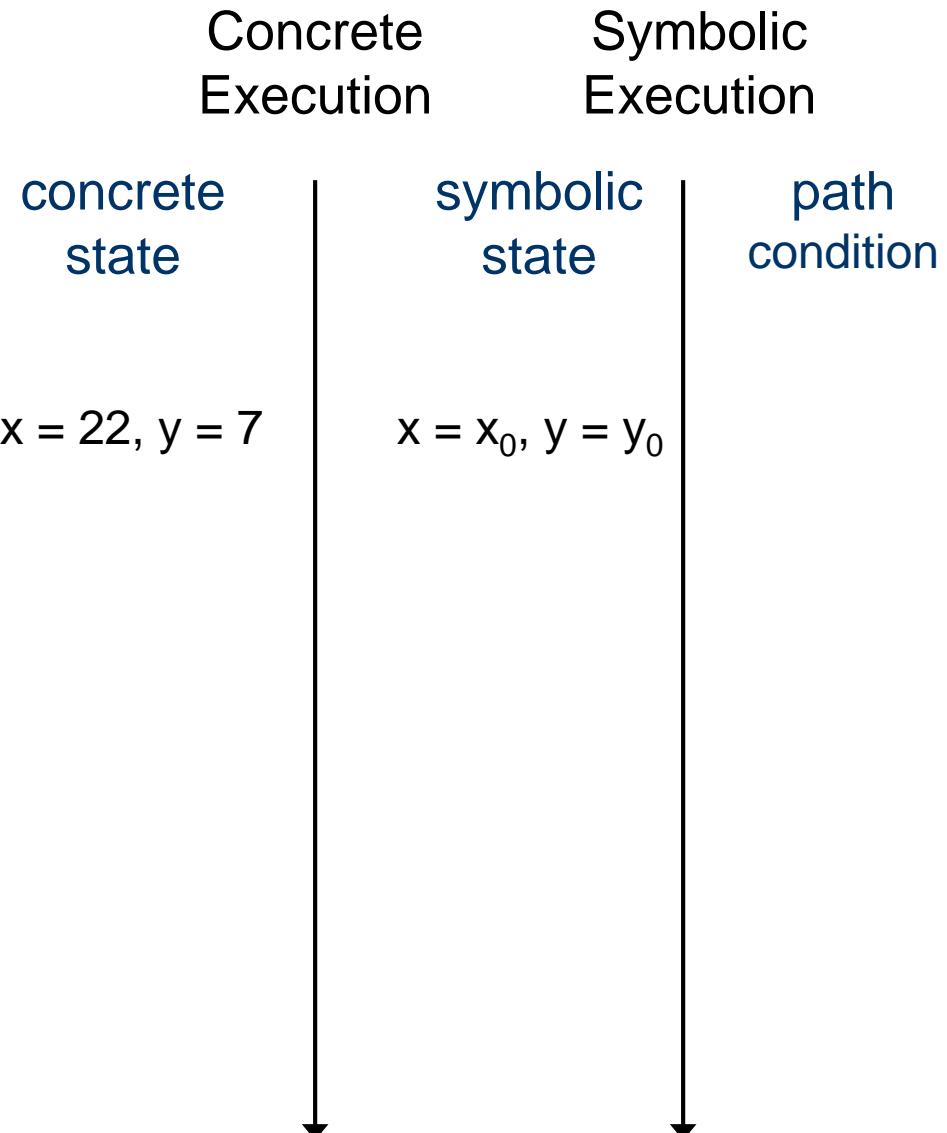
```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```



Novelty : Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;  
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

ERROR;

```
}
```

```
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

path
condition

Solve: $(y_0 * y_0) \% 50 == x_0$

Don't know how to solve!

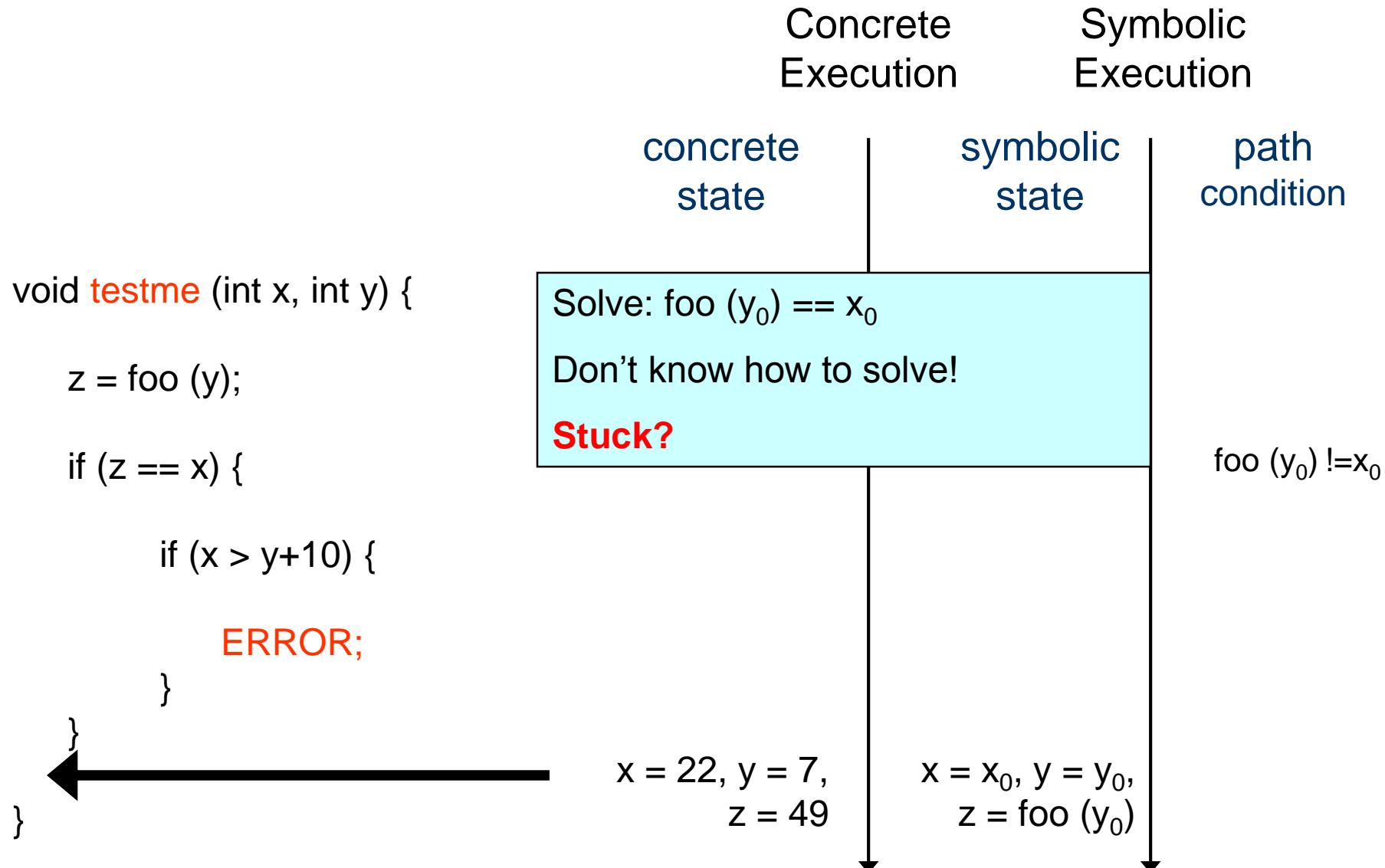
Stuck?

$(y_0 * y_0) \% 50 != x_0$

$x = 22, y = 7,$
 $z = 49$

$x = x_0, y = y_0,$
 $z = (y_0 * y_0) \% 50$

Novelty : Simultaneous Concrete and Symbolic Execution



Novelty : Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;  
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

path
condition

Solve: $(y_0 * y_0) \% 50 == x_0$

Don't know how to solve!

Not Stuck!

Use concrete state

Replace y_0 by 7 (sound)

$(y_0 * y_0) \% 50 != x_0$

$x = 22, y = 7,$
 $z = 49$

$x = x_0, y = y_0,$
 $z = (y_0 * y_0) \% 50$

Novelty : Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;  
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

path
condition

Solve: $49 == x_0$

Solution : $x_0 = 49, y_0 = 7$

$49 \neq x_0$

$x = 22, y = 7,$
 $z = 48$

$x = x_0, y = y_0,$
 $z = 49$

Novelty : Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

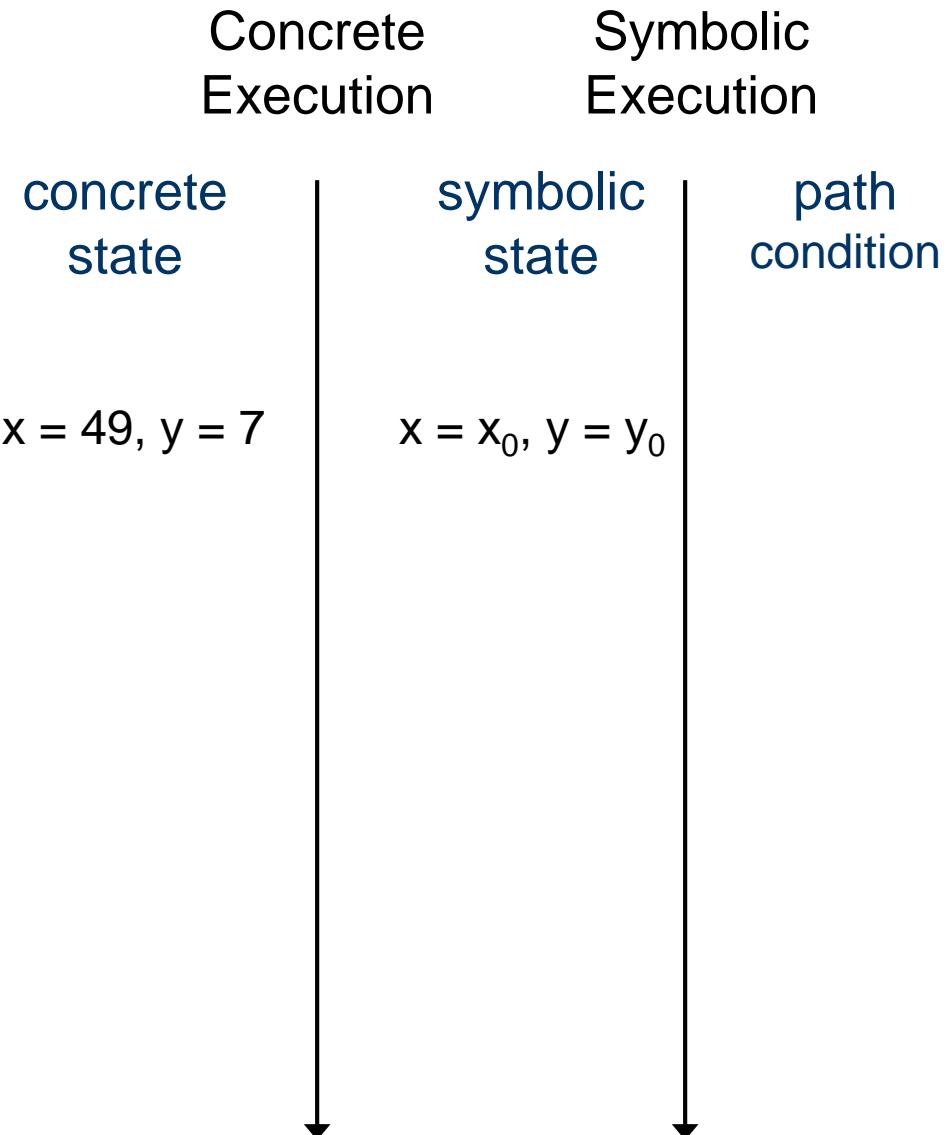
```
        if (x > y+10) {
```

```
            ERROR;
```

```
}
```

```
}
```

```
}
```



Novelty : Simultaneous Concrete and Symbolic Execution

```
int foo (int v) {
```

```
    return (v*v) % 50;
```

```
}
```

```
void testme (int x, int y) {
```

```
    z = foo (y);
```

```
    if (z == x) {
```

```
        if (x > y+10) {
```

```
            ← ERROR;
```

```
}
```

```
}
```

Concrete
Execution

Symbolic
Execution

path
condition

concrete

symbolic
state

Program Error

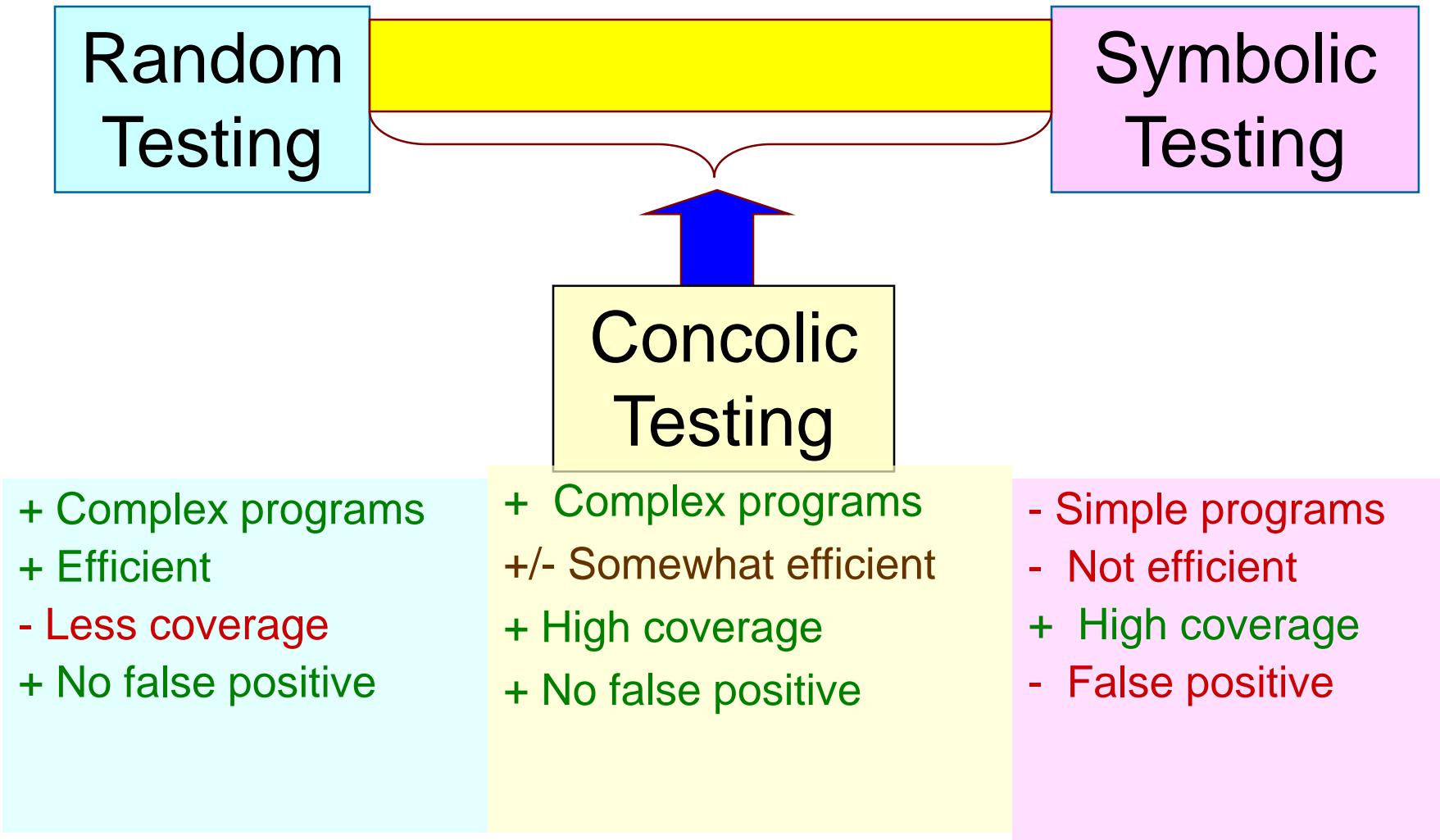
$x = 49, y = 7,$
 $z = 49$

$x = x_0, y = y_0,$
 $z = 49$

$2*y_0 == x_0$

$x_0 > y_0 + 10$

Concolic Testing: A Middle Approach



Implementations

- DART and CUTE for C programs
- jCUTE for Java programs
 - Goto <http://srl.cs.berkeley.edu/~ksen/> for CUTE and jCUTE binaries
- MSR has four implementations
 - SAGE, PEX, YOGI, Vigilante
- Similar tool: EXE at Stanford
- Easiest way to use and to develop on top of CUTE
 - Implement concolic testing yourself

Testing Data Structures

(joint work with Darko Marinov and
Gul Agha

Example

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```

- Random Test Driver:

- random memory graph
reachable from p
- random value for x

- Probability of reaching `abort()` is
extremely low

CUTE Approach

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
}
```

```
int testme(cell *p, int x) {  
    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```

Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

constraints

p
NULL , x=236

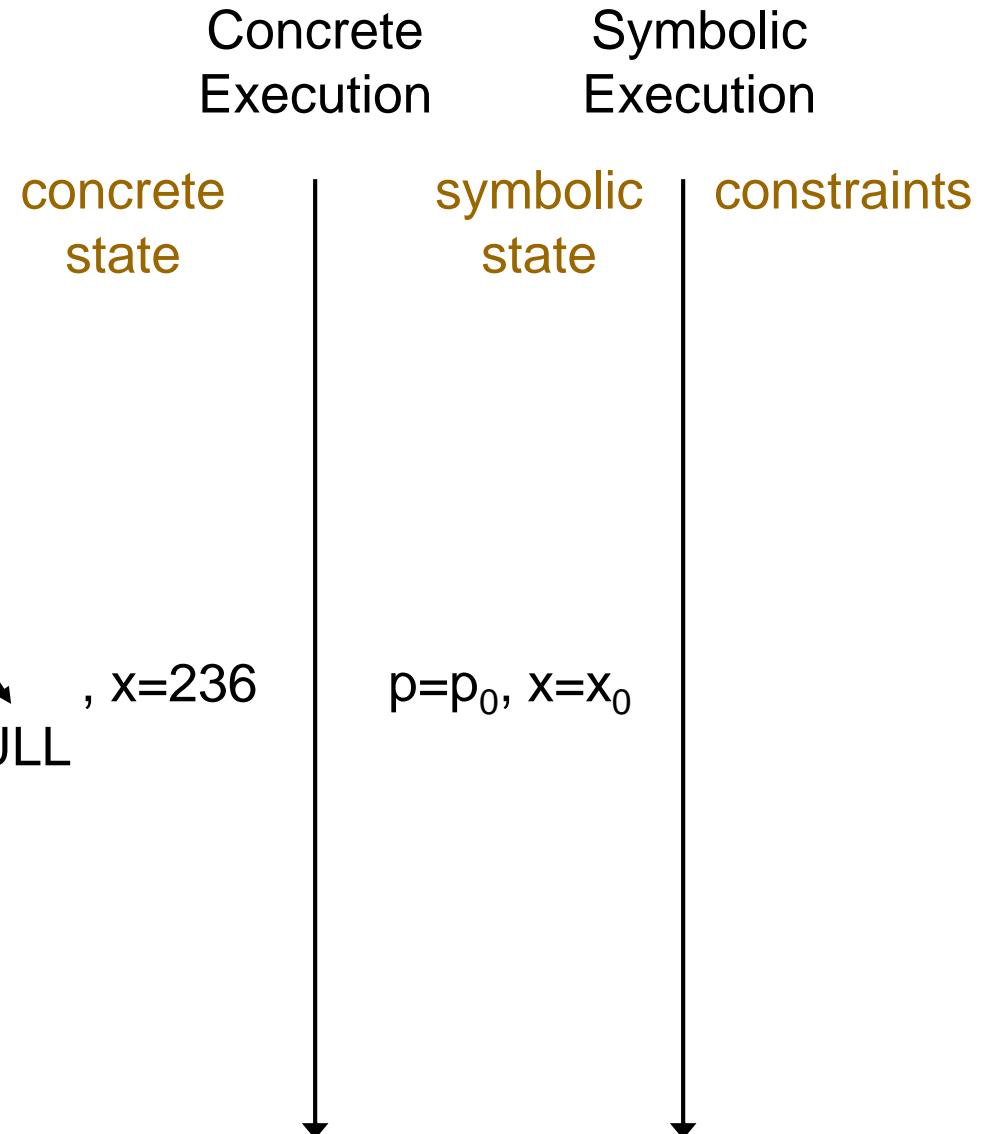
$p=p_0, x=x_0$

CUTE Approach

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
    return 2*v + 1;  
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        if (p != NULL)  
            if (f(x) == p->v)  
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                    abort();  
    return 0;  
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```



CUTE Approach

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    int v;  
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} cell;
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int f(int v) {  
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    if (x > 0)  
        if (p != NULL)  
            if (f(x) == p->v)  
                if (p->next == p)  
                    abort();  
    return 0;  
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

constraints

←
p
NULL , x=236

p=p₀, x=x₀

x₀>0

CUTE Approach

```
typedef struct cell {  
    int v;  
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} cell;
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int f(int v) {  
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int testme(cell *p, int x) {  
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    return 0;  
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

constraints

$x_0 > 0$

$(p_0 \neq \text{NULL})$

\leftarrow
 p
NULL , $x=236$

$p=p_0, x=x_0$

CUTE Approach

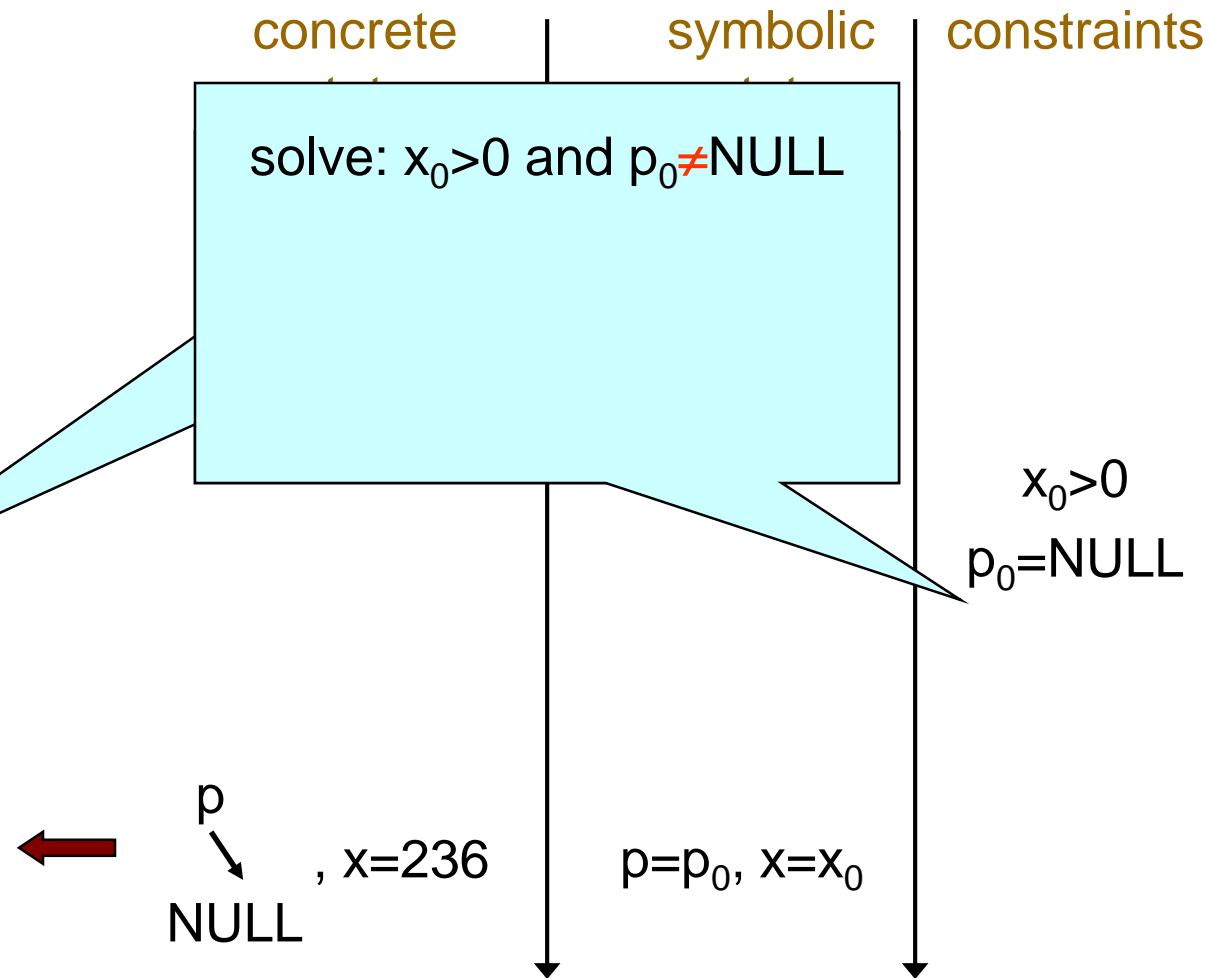
```
typedef struct cell {
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    return 2*v + 1;
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                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution



CUTE Approach

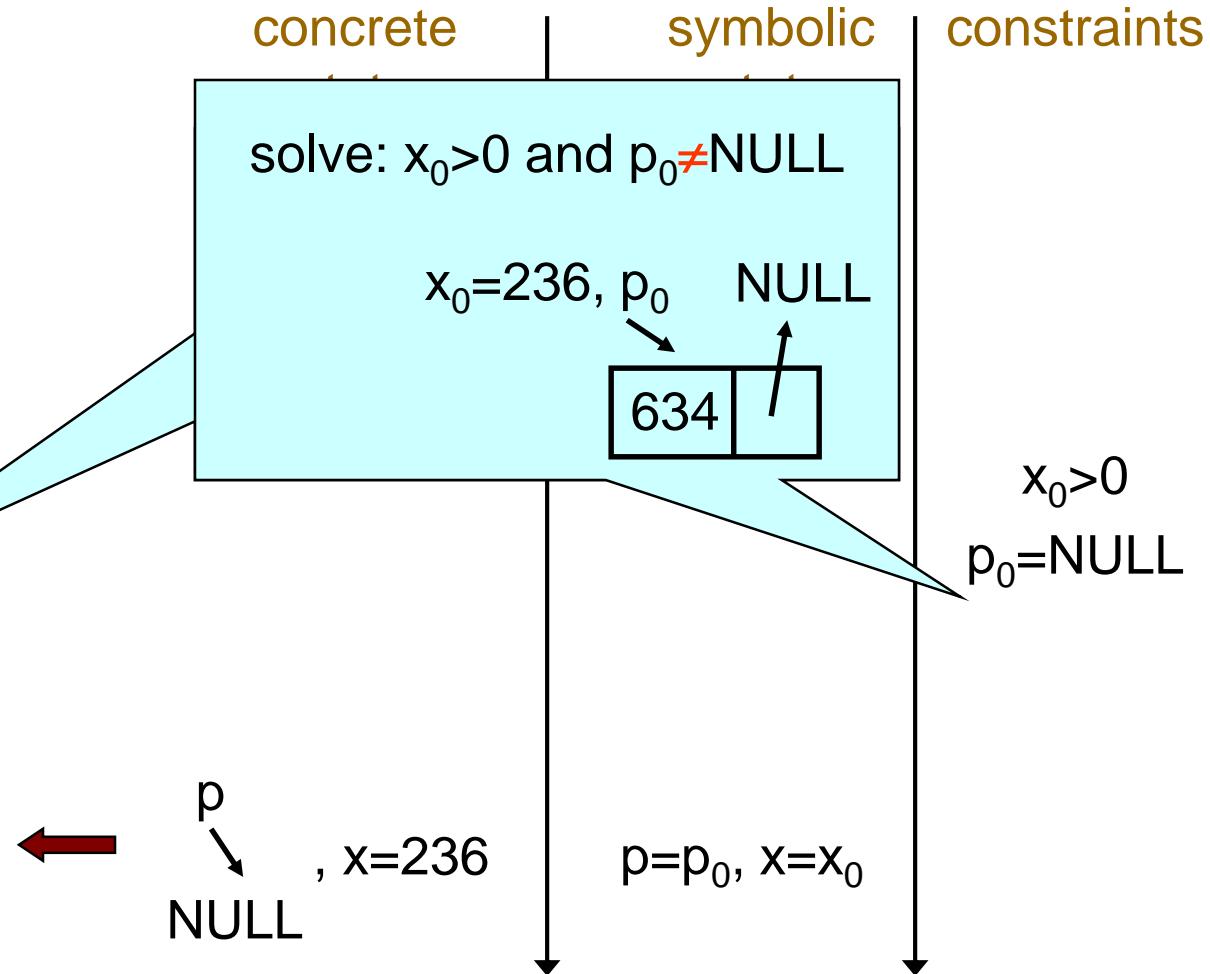
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typedef struct cell {
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```

Concrete
Execution

Symbolic
Execution



CUTE Approach

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typedef struct cell {  
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    return 0;  
}
```

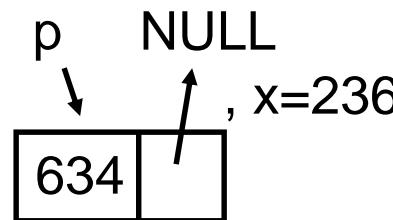
Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

constraints



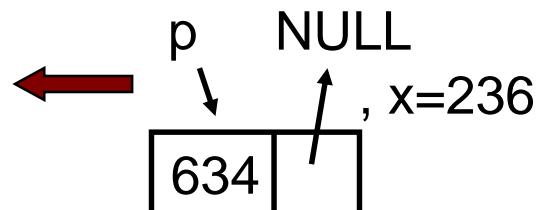
$p=p_0, x=x_0,$
 $p->v=v_0,$
 $p->next=n_0$

CUTE Approach

```
typedef struct cell {  
    int v;  
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int f(int v) {  
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                if (p->next == p)  
                    abort();  
    return 0;  
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```



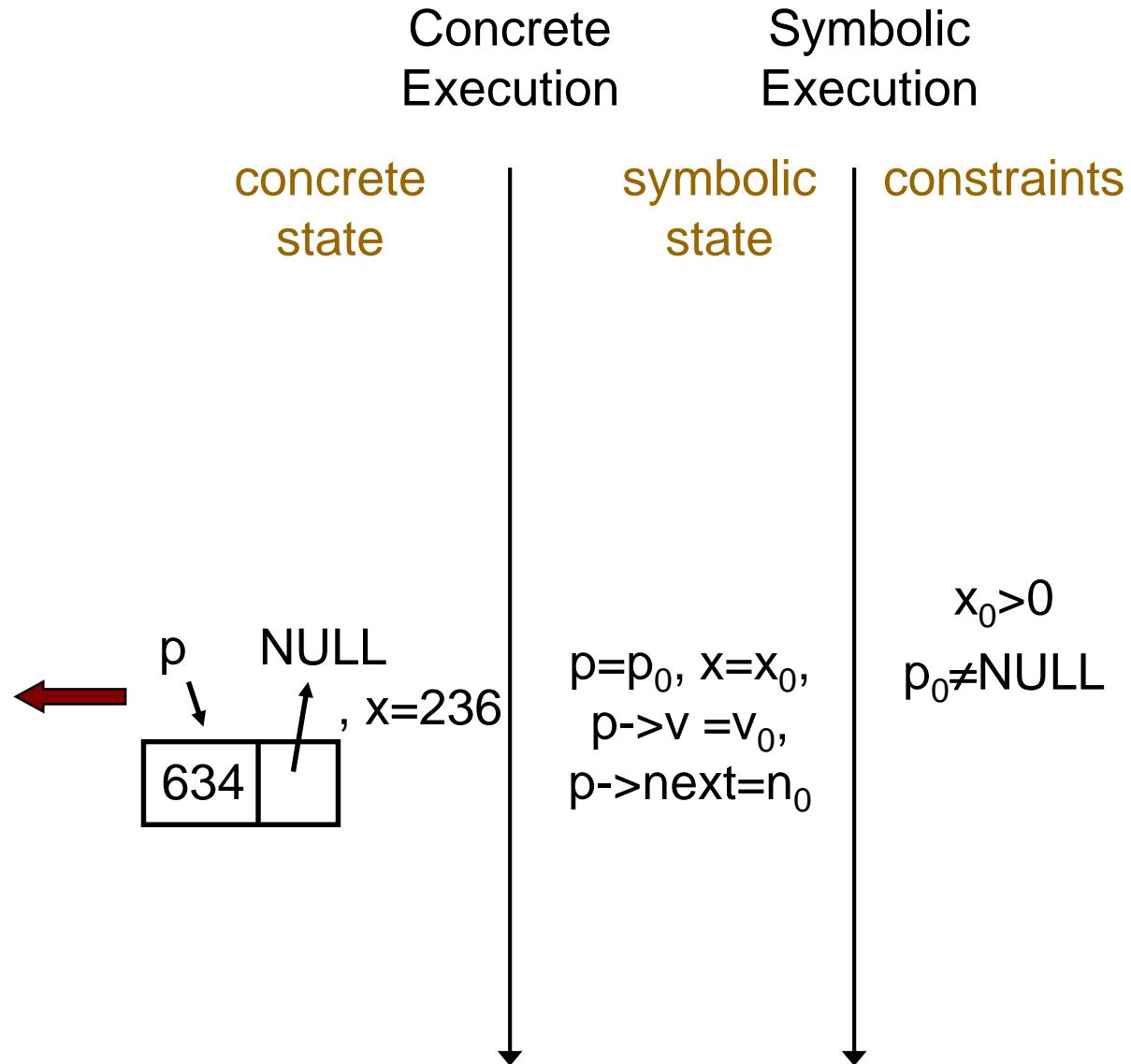
Concrete Execution	Symbolic Execution	constraints
concrete state	symbolic state	
$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$		$x_0 > 0$

CUTE Approach

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

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int f(int v) {
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```
int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
    return 0;
}
```

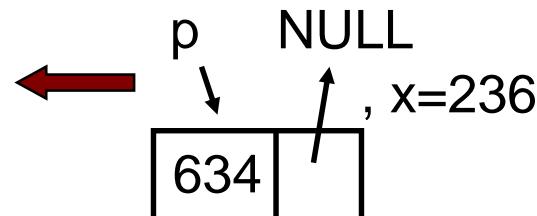


CUTE Approach

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
```

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int f(int v) {
    return 2*v + 1;
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int testme(cell *p, int x) {
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```



Concrete Execution	Symbolic Execution	constraints
concrete state	symbolic state	
		$x_0 > 0$
		$p_0 \neq \text{NULL}$
		$2x_0 + 1 \neq v_0$

CUTE Approach

```
typedef struct cell {
    int v;
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                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

concrete
state

Symbolic
Execution

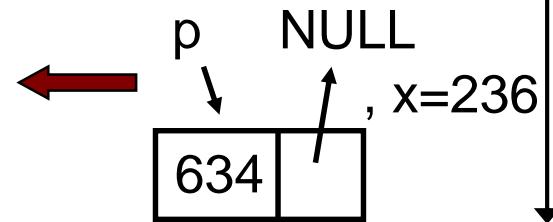
symbolic
state

constraints

$$x_0 > 0$$

$$p_0 \neq \text{NULL}$$

$$2x_0 + 1 \neq v_0$$



$$\begin{aligned} p &= p_0, \\ x &= x_0, \\ p->v &= v_0, \\ p->next &= n_0 \end{aligned}$$

CUTE Approach

```
typedef struct cell {
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                if (p->next == p)
                    abort();
    return 0;
}
```

Concrete
Execution

Symbolic
Execution

concrete

symbolic

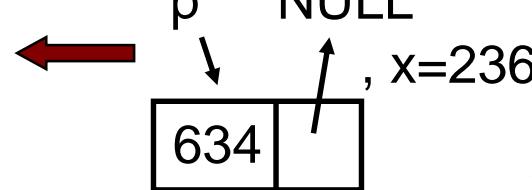
constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$
and $2x_0 + 1 = v_0$

$$x_0 > 0$$

$$p_0 \neq \text{NULL}$$

$$2x_0 + 1 \neq v_0$$



$$\begin{aligned} p &= p_0, x = x_0, \\ p->v &= v_0, \\ p->\text{next} &= n_0 \end{aligned}$$

CUTE Approach

```
typedef struct cell {
    int v;
    struct cell *next;
} cell;
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int f(int v) {
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int testme(cell *p, int x) {
    if (x > 0)
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```

Concrete
Execution

Symbolic
Execution

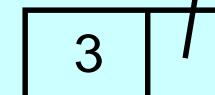
constraints

concrete

symbolic

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$
and $2x_0 + 1 = v_0$

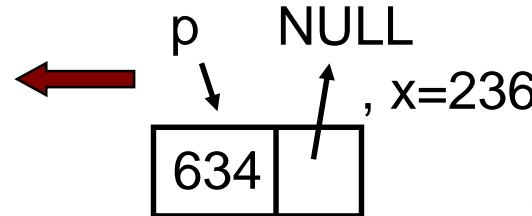
$x_0 = 1, p_0$ NULL



$x_0 > 0$

$p_0 \neq \text{NULL}$

$2x_0 + 1 \neq v_0$



$p = p_0, x = x_0,$
 $p->v = v_0,$
 $p->next = n_0$

CUTE Approach

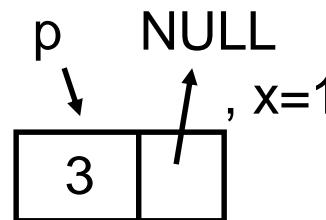
```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

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int f(int v) {  
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```

Concrete
Execution

concrete
state



Symbolic
Execution

symbolic
state

$p=p_0, x=x_0,$
 $p->v=v_0,$
 $p->next=n_0$

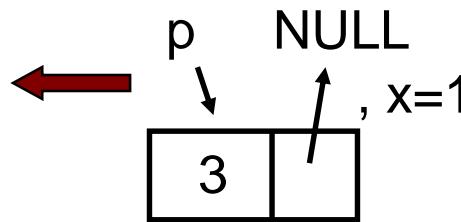
constraints

CUTE Approach

```
typedef struct cell {  
    int v;  
    struct cell *next;  
} cell;
```

```
int f(int v) {  
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Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

constraints

$p=p_0, x=x_0,$
 $p->v=v_0,$
 $p->next=n_0$

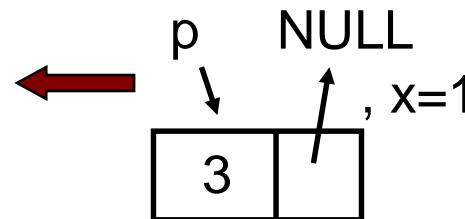
$x_0>0$

CUTE Approach

```
typedef struct cell {  
    int v;  
    struct cell *next;  
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```

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int f(int v) {  
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                if (p->next == p)  
                    abort();  
    return 0;  
}
```



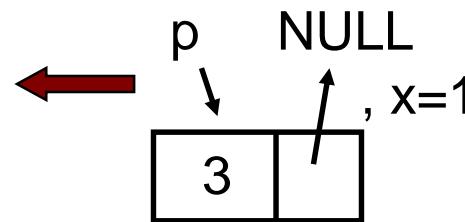
Concrete Execution	Symbolic Execution	constraints
concrete state	symbolic state	
	$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$	$x_0 > 0$ $p_0 \neq \text{NULL}$

CUTE Approach

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typedef struct cell {
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```



Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

constraints

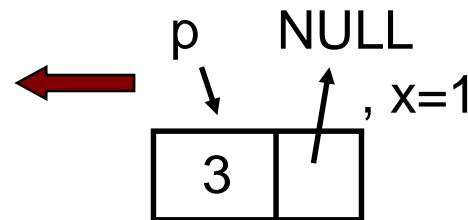
$x_0 > 0$
 $p_0 \neq \text{NULL}$
 $2x_0 + 1 = v_0$

CUTE Approach

```
typedef struct cell {
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int f(int v) {
    return 2*v + 1;
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int testme(cell *p, int x) {
    if (x > 0)
        if (p != NULL)
            if (f(x) == p->v)
                if (p->next == p)
                    abort();
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}
```



Concrete Execution	Symbolic Execution	
concrete state	symbolic state	constraints
		$x_0 > 0$
		$p_0 \neq \text{NULL}$
		$2x_0 + 1 = v_0$
		$n_0 \neq p_0$

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typedef struct cell {
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```

Concrete
Execution

concrete
state

Symbolic
Execution

symbolic
state

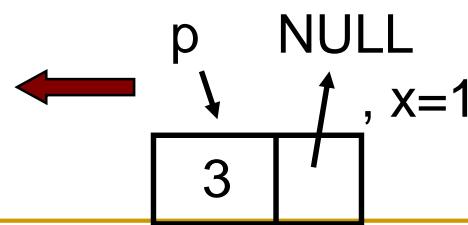
constraints

$$x_0 > 0$$

$$p_0 \neq \text{NULL}$$

$$2x_0 + 1 = v_0$$

$$n_0 \neq p_0$$



$$\begin{aligned} p &= p_0, \\ x &= x_0, \\ p->v &= v_0, \\ p->next &= n_0 \end{aligned}$$

CUTE Approach

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typedef struct cell {
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int f(int v) {
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Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

constraints

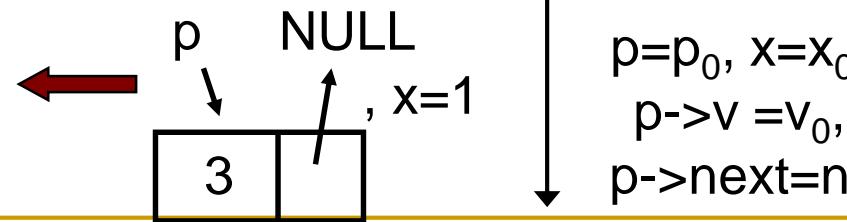
solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$
and $2x_0 + 1 = v_0$ and $n_0 = p_0$

$x_0 > 0$

$p_0 \neq \text{NULL}$

$2x_0 + 1 = v_0$

$n_0 \neq p_0$



CUTE Approach

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typedef struct cell {
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Concrete
Execution

Symbolic
Execution

concrete
state

symbolic
state

constraints

solve: $x_0 > 0$ and $p_0 \neq \text{NULL}$
and $2x_0 + 1 = v_0$ and $n_0 = p_0$

$$x_0 = 1, p_0$$

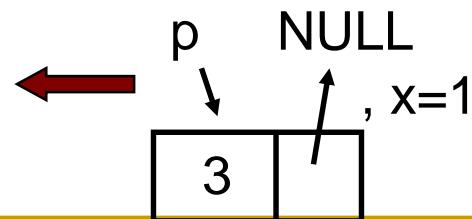


$$x_0 > 0$$

$$p_0 \neq \text{NULL}$$

$$2x_0 + 1 = v_0$$

$$n_0 \neq p_0$$



$$\begin{aligned} p &= p_0, x = x_0, \\ p->v &= v_0, \\ p->next &= n_0 \end{aligned}$$

CUTE Approach

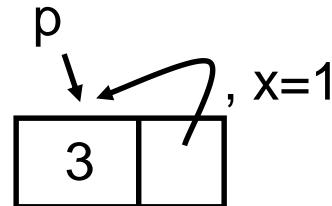
```
typedef struct cell {  
    int v;  
    struct cell *next;  
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Concrete
Execution

concrete
state



Symbolic
Execution

symbolic
state

$p=p_0, x=x_0,$
 $p->v=v_0,$
 $p->next=n_0$

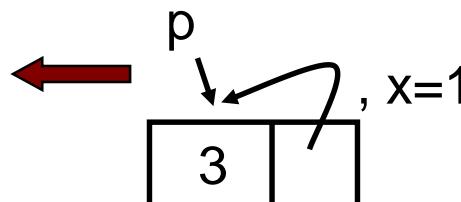
constraints

CUTE Approach

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typedef struct cell {  
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Concrete
Execution
concrete
state

Symbolic
Execution
symbolic
state

constraints

$$p=p_0, x=x_0, \\ p->v=v_0, \\ p->next=n_0$$

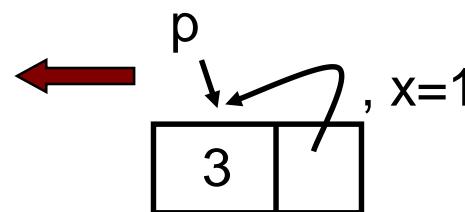
$$x_0 > 0$$

CUTE Approach

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typedef struct cell {  
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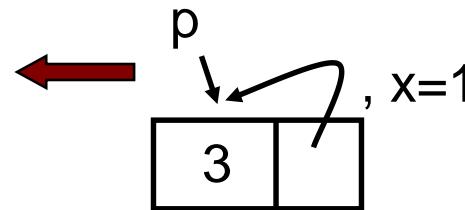
Concrete Execution	Symbolic Execution	constraints
concrete state	symbolic state	
	$p=p_0, x=x_0,$ $p->v=v_0,$ $p->next=n_0$	$x_0 > 0$ $p_0 \neq \text{NULL}$

CUTE Approach

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typedef struct cell {  
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}
```



Concrete Execution	Symbolic Execution	constraints
concrete state	symbolic state	$x_0 > 0$
		$p_0 \neq \text{NULL}$

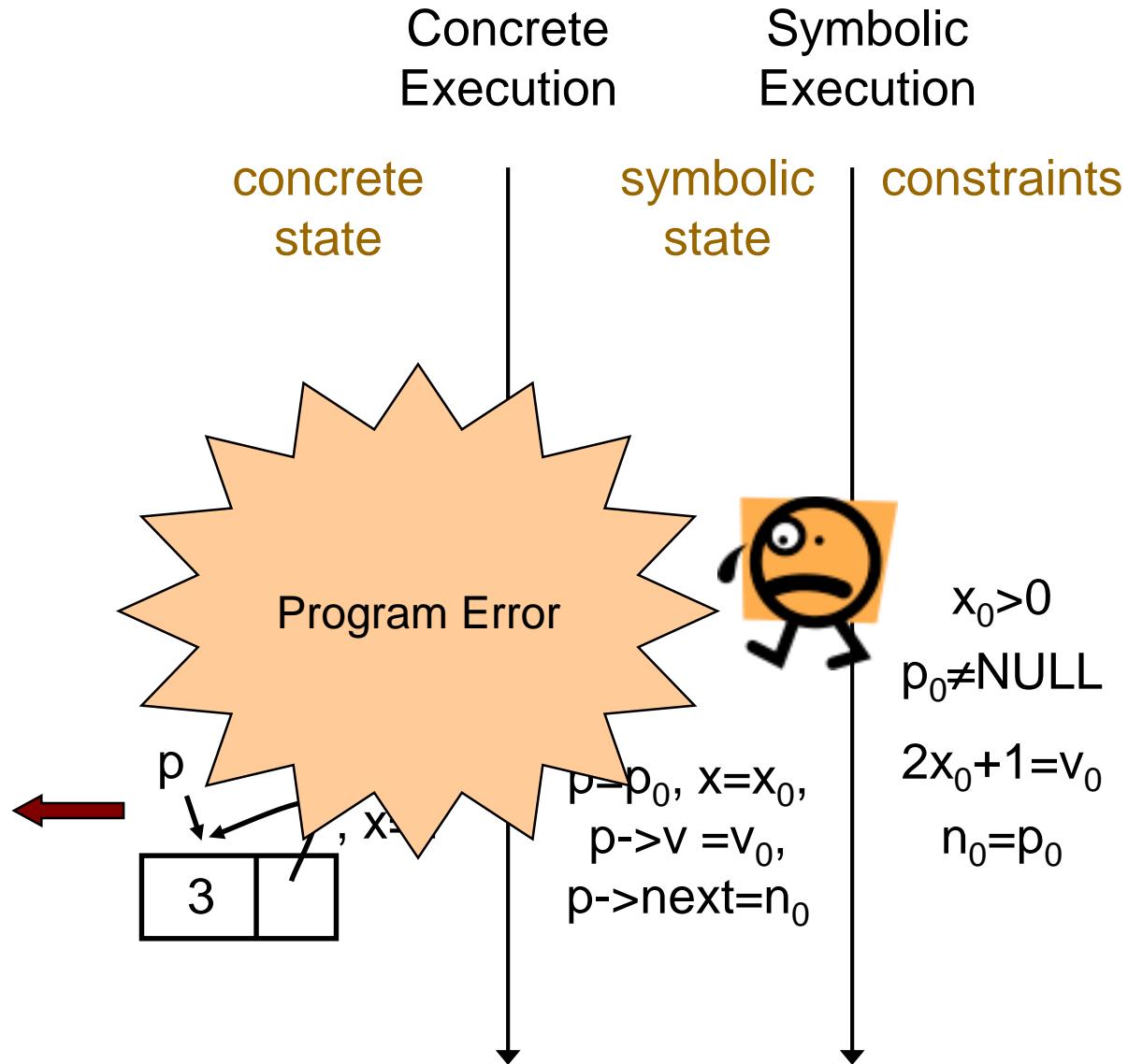
$$p=p_0, x=x_0, \\ p->v=v_0, \\ p->next=n_0$$

CUTE Approach

```
typedef struct cell {  
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CUTE in a Nutshell

- Generate concrete inputs one by one
 - each input leads program along a different path

CUTE in a Nutshell

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- On each input execute program both **concretely** and **symbolically**

CUTE in a Nutshell

- Generate concrete inputs one by one
 - each input leads program along a different path
- On each input execute program both **concretely** and **symbolically**
 - Both **cooperate** with each other
 - concrete execution **guides** the symbolic execution

CUTE in a Nutshell

- Generate concrete inputs one by one
 - each input leads program along a different path
- On each input execute program both **concretely** and **symbolically**
 - Both **cooperate** with each other
 - concrete execution **guides** the symbolic execution
 - concrete execution **enables** symbolic execution to overcome incompleteness of theorem prover
 - replace symbolic expressions by concrete values if symbolic expressions become complex
 - resolve aliases for pointer using concrete values
 - handle arrays naturally

CUTE in a Nutshell

- Generate concrete inputs one by one
 - each input leads program along a different path
- On each input execute program both **concretely** and **symbolically**
 - Both **cooperate** with each other
 - concrete execution **guides** the symbolic execution
 - concrete execution **enables** symbolic execution to overcome incompleteness of theorem prover
 - replace symbolic expressions by concrete values if symbolic expressions become complex
 - resolve aliases for pointer using concrete values
 - handle arrays naturally
 - symbolic execution **helps to generate** concrete input for next execution
 - increases coverage

Data-structure Testing

Solving Data-structure Invariants

```
int isSortedSlist(slist * head) {
    slist * cur, *tmp;
    int i,j;
    if (head == 0) return 1;
    i=j=0;
    for (cur = head; cur!=0; cur = cur->next){
        i++;
        j=1;
        for (tmp = head; j<i; tmp = tmp->next){
            j++;
            if(cur==tmp) return 0;
        }
    }
    for (cur = head; cur->next!=0; cur =
         >next){
        if(cur->i > cur->_next->i) return 0;
    }
    return 1;
}
```

```
testme(slist *L,slist *e){
    CUTE_assume(isSortedSlist(L));
    sglib_slist_add(&L,e);
    CUTE_assert(isSortedSlist(L));
}
```

Data-structure Testing

Generating Call Sequence

```
for (i=1; i<10; i++) {  
    CU_input(toss);  
    CU_input(e);  
    switch(toss){  
        case 2:      sglib_hashed_ilist_add_if_not_member(htab,e,&m);  
        break;  
        case 3:      sglib_hashed_ilist_delete_if_member(htab,e,&m);  
        break;  
        case 4:      sglib_hashed_ilist_delete(htab,e); break;  
        case 5:      sglib_hashed_ilist_is_member(htab,e); break;  
        case 6:      sglib_hashed_ilist_find_member(htab,e); break;  
    }  
}
```



抽象解释



抽象解释

- 用于论证抽象正确性的理论
- 相当数量的文献采用抽象解释来论证正确性
- 转向使用Alex Aiken的课程胶片



课后作业

- 简答：如果用抽象解释理论论证数据流分析的安全性，抽象域、具体域和 σ 、 μ 、 α 、 γ 分别是什么？符号执行呢？
 - 简述概念即可，不需要写出形式定义